

# Homework Six, Physics 242, Spring 2009

## Due Friday, June 12

[1.] Solve *either* the one site Kondo *or* the one site Anderson Hamiltonian. That is, compute all the eigenenergies of the 8 (Kondo) or 16 (Anderson) dimensional Hilbert space.

$$H_{\text{Kondo}}^{1 \text{ site}} = \frac{J}{2} \left[ S^z (c_{\uparrow}^{\dagger} c_{\uparrow} - c_{\downarrow}^{\dagger} c_{\downarrow}) + S^+ c_{\downarrow}^{\dagger} c_{\uparrow} + S^- c_{\uparrow}^{\dagger} c_{\downarrow} \right]. \quad (1)$$

Here  $S$  is a spin-1/2 operator and  $c, c^{\dagger}$  are fermion destruction(creation) operators.

$$H_{\text{Anderson}}^{1 \text{ site}} = V \sum_{\sigma} (c_{\sigma}^{\dagger} d_{\sigma} + d_{\sigma}^{\dagger} c_{\sigma}) + U d_{\uparrow}^{\dagger} d_{\uparrow} d_{\downarrow}^{\dagger} d_{\downarrow} + E_d (d_{\uparrow}^{\dagger} d_{\uparrow} + d_{\downarrow}^{\dagger} d_{\downarrow}). \quad (2)$$

Here  $c, c^{\dagger}$  and  $d, d^{\dagger}$  are fermion destruction(creation) operators. Note: You may encounter (cubic) equations which are not analytically tractable. If that happens, just leave the characteristic equation as a cubic or whatever. It may be that a special choice of  $E_d$  (such as  $E_d = U/2$ ) makes the mathematics more simple for the Anderson case. (This is called the ‘symmetric’ form of the model and has some special properties.)

[2.] Discuss (two paragraphs) the nature of the magnetic order in the iron pnictides. Which atoms are magnetic? What is their moment? How are the moments aligned (antiferromagnetic? ferromagnetic?). What is(are) numerical value(s) for the exchange constant(s)? What is the magnetic transition temperature? What experiments give this information?